

SUMMER PACKET 2025 - 2026 CONWELL-EGAN CATHOLIC HIGH SCHOOL



This summer assignment is a review and exploration of key skills that are necessary for success in your mathematics course as well as future high school mathematics courses.

All summer packets are due on the Friday of the first full week of school.

EXPRESSIONS AND FORMULAS

EXAMPLE Evaluate Algebraic Expressions **a**. Evaluate $m + (n - 1)^2$ if m = 3 and n = -4. $m + (n - 1)^2 = 3 + (-4 - 1)^2$ Replace *m* with 3 and *n* with -4. $= 3 + (-5)^2$ Add -4 and -1. = 3 + 25 Find $(-5)^2$. = 28Add 3 and 25. **b.** Evaluate $x^2 - y(x + y)$ if x = 8 and y = 1.5. $x^2 - y(x + y) = 8^2 - 1.5(8 + 1.5)$ Replace x with 8 and y with 1.5. $= 8^2 - 1.5(9.5)$ Add 8 and 1.5. = 64 - 1.5(9.5) Find 8². = 64 - 14.25 Multiply 1.5 and 9.5. = 49.75Subtract 14.25 from 64. **c.** Evaluate $\frac{a^3 + 2bc}{c^2 - 5}$ if a = 2, b = -4, and c = -3. $\frac{a^3 + 2bc}{c^2 - 5} = \frac{2^3 + 2(-4)(-3)}{(-3)^2 - 5} \quad a = 2, b = -4, \text{ and } c = -3$ $= \frac{8 + (-8)(-3)}{9 - 5}$ Evaluate the numerator and the denominator separately. $=\frac{8+24}{9-5}$ Multiply -8 by -3. $=\frac{32}{4}$ or 8 Simplify the numerator and the denominator. Then divide.

Evaluate each expression if $q = \frac{1}{2}$, r = 1.2, s = -6, and t = 5.

1 . $qr - st$	2. $qr \div st$	3. qrst	4. $qr + st$
5. $\frac{3q}{4s}$	6. $\frac{5qr}{t}$	7. $\frac{2r(4s-1)}{t}$	8. $\frac{4q^3s+1}{t-1}$

Evaluate each expression if a = -0.5, b = 4, c = 5, and d = -3.

9. 3b + 4d10. $ab^2 + c$ 11. $bc + d \div a$ 12. 7ab - 3d13. $ad + b^2 - c$ 14. $\frac{4a + 3c}{3b}$ 15. $\frac{3ab^2 - d^3}{a}$ 16. $\frac{5a + ad}{bc}$

PROPERTIES OF REAL NUMBERS

EXAMPLE Identify Properties of Real Numbers

Name the property illustrated by (5 + 7) + 8 = 8 + (5 + 7).

Commutative Property of Addition

The Commutative Property says that the order in which you add does not change the sum.

EXAMPLE Simplify an Expression

Simplify 2(5m + n) + 3(2m - 4n).2(5m + n) + 3(2m - 4n)= 2(5m) + 2(n) + 3(2m) - 3(4n)= 10m + 2n + 6m - 12n= 10m + 6m + 2n - 12n= 10m + 6m + 2n - 12n= (10 + 6)m + (2 - 12)n= 16m - 10nSimplify.

KEY CONCEPT

Real Number Properties

For any real numbers <i>a</i> , <i>b</i> , and <i>c</i> :		
Property	Addition Multiplication	
Commutative	a + b = b + a	$a \cdot b = b \cdot a$
Associative	(a + b) + c = a + (b + c)	$(a \cdot b) \cdot c = a \cdot (b \cdot c)$
Identity	a + 0 = a = 0 + a	$a \cdot 1 = 1 \cdot a$
Inverse	a + (-a) = 0 = (-a) + a	If $a \neq 0$, then $a \cdot \frac{1}{a} = 1 = \frac{1}{a} \cdot a$.
Distributive	a(b+c) = ab + ac and (b+c)a = ba + ca	

Name the sets of numbers to which each number belongs. (Use N, W, Z, Q, I, and R.)

1. 8.2
 2. -9
 3.
$$\sqrt{36}$$

 4. $-\frac{1}{3}$
 5. $\sqrt{2}$
 6. $-0.\overline{24}$

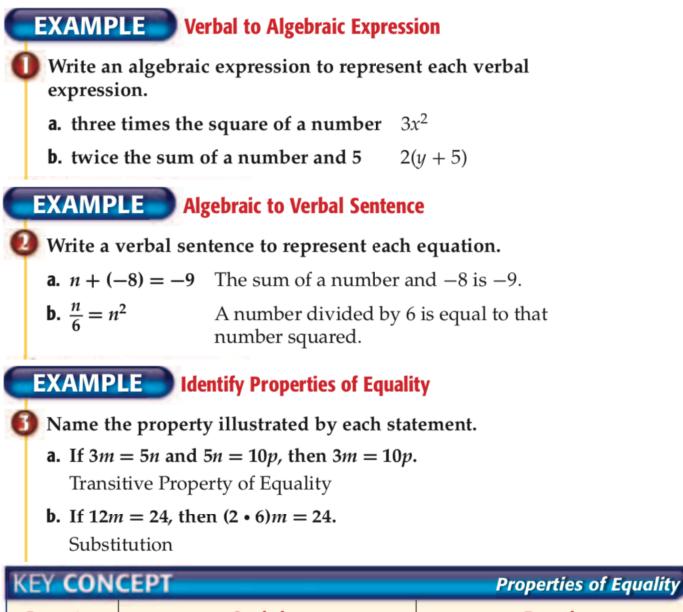
Name the property illustrated by each equation.

7. (4+9a)2b = 2b(4+9a)8. $3(\frac{1}{3}) = 1$ 9. $a(3-2) = a \cdot 3 - a \cdot 2$ 10. (-3b) + 3b = 011. jk + 0 = jk12. (2a)b = 2(ab)

Simplify each expression.

13. 7s + 9t + 2s - 7t **14.** 6(2a + 3b) + 5(3a - 4b) **15.** 4(3x - 5y) - 8(2x + y) **16.** 0.2(5m - 8) + 0.3(6 - 2m) **17.** $\frac{1}{2}(7p + 3q) + \frac{3}{4}(6p - 4q)$ **18.** $\frac{4}{5}(3v - 2w) - \frac{1}{5}(7v - 2w)$

SOLVING EQUATIONS



KET CUNCEPT		Properties of Equality
Property	Symbols	Examples
Reflexive	For any real number $a, a = a$.	-7 + n = -7 + n
Symmetric	For all real numbers a and b , if $a = b$, then $b = a$.	If $3 = 5x - 6$, then $5x - 6 = 3$.
Transitive	For all real numbers a , b , and c , if $a = b$ and $b = c$, then $a = c$.	If $2x + 1 = 7$ and $7 = 5x - 8$, then $2x + 1 = 5x - 8$.
Substitution	If $a = b$, then a may be replaced by b and b may be replaced by a .	If $(4 + 5)m = 18$, then $9m = 18$.

EXAMPLE Solve One-Step Equations

Solve each equation. Check your solution.

a. a + 4.39 = 76a + 4.39 = 76 Original equation a + 4.39 - 4.39 = 76 - 4.39 Subtract 4.39 from each side. a = 71.61 Simplify.

The solution is 71.61.

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CHECK a + 4.39 = 76 Original equation **71.61** + 4.39 $\stackrel{?}{=} 76$ Substitute 71.61 for *a*. $76 = 76 \checkmark$ Simplify.

b.
$$-\frac{3}{5}d = 18$$

 $-\frac{3}{5}d = 18$ Original equation
 $-\frac{5}{3}\left(-\frac{3}{5}\right)d = -\frac{5}{3}(18)$ Multiply each side by $-\frac{5}{3}$, the multiplicative inverse of $-\frac{3}{5}$.
 $d = -30$ Simplify.

The solution is -30.

CHECK $-\frac{3}{5}d = 18$ Original equation $-\frac{3}{5}(-30) \stackrel{?}{=} 18$ Substitute -30 for *d*. $18 = 18 \checkmark$ Simplify.

EXAMPLE Solve a Multi-Step Equation

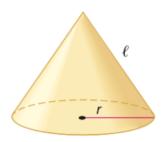
Solve
$$2(2x + 3) - 3(4x - 5) = 22$$
.
 $2(2x + 3) - 3(4x - 5) = 22$ Original equation
 $4x + 6 - 12x + 15 = 22$ Apply the Distributive Property.
 $-8x + 21 = 22$ Simplify the left side.
 $-8x = 1$ Subtract 21 from each side to isolate the variable.
 $x = -\frac{1}{8}$ Divide each side by -8 .

The solution is $-\frac{1}{8}$.

EXAMPLE Solve for a Variable

GEOMETRY The formula for the surface area *S* of a cone is $S = \pi r \ell + \pi r^2$, where ℓ is the slant height of the cone and *r* is the radius of the base. Solve the formula for ℓ .

 $S = \pi r \ell + \pi r^2$ Surface area formula $S - \pi r^2 = \pi r \ell + \pi r^2 - \pi r^2$ Subtract πr^2 from each side. $S - \pi r^2 = \pi r \ell$ Simplify. $\frac{S - \pi r^2}{\pi r} = \frac{\pi r \ell}{\pi r}$ Divide each side by πr . $\frac{S - \pi r^2}{\pi r} = \ell$ Simplify.



KEY CONCEPT

Properties of Equality

Addition and Subtraction

Symbols For any real numbers *a*, *b*, and *c*, if a = b, then a + c = b + c and a - c = b - c.

Examples If x - 4 = 5, then x - 4 + 4 = 5 + 4. If n + 3 = -11, then n + 3 - 3 = -11 - 3.

Multiplication and Division

Symbols For any real numbers *a*, *b*, and *c*, if a = b, then $a \cdot c = b \cdot c$, and if $c \neq 0$, $\frac{a}{c} = \frac{b}{c}$. **Examples** If $\frac{m}{4} = 6$, then $4 \cdot \frac{m}{4} = 4 \cdot 6$. If -3y = 6, then $\frac{-3y}{-3} = \frac{6}{-3}$.

Write an algebraic expression to represent each verbal expression.

- 1. twelve decreased by the square of a number
- **3**. the product of the square of a number and 6
- **2**. twice the sum of a number and negative nine
- 4. the square of the sum of a number and 11

Name the property illustrated by each statement.

- 5. If a + 1 = 6, then 3(a + 1) = 3(6).
- 7. If 7x = 42, then 7x 5 = 42 5.
- 6. If x + (4 + 5) = 21, then x + 9 = 21.
- 8. If 3 + 5 = 8 and $8 = 2 \cdot 4$, then $3 + 5 = 2 \cdot 4$.

Solve each equation. Check your solution.

9. 5t + 8 = 8810. 27 - x = -411. $\frac{3}{4}y = \frac{2}{3}y + 5$ 12. 8s - 3 = 5(2s + 1)13. 3(k - 2) = k + 414. 0.5z + 10 = z + 415. $8q - \frac{q}{3} = 46$ 16. $-\frac{2}{7}r + \frac{3}{7} = 5$ 17. $d - 1 = \frac{1}{2}(d - 2)$

Solve each equation or formula for the specified variable.

18. $C = \pi r$; for r **19.** I = Prt, for t **20.** $m = \frac{n-2}{n}$, for n

SOLVING ABSOLUTE-VALUE EQUATIONS

EXAMPLE Evaluate an Expression with Absolute Value D Evaluate 1.4 + |5y - 7| if y = -3. 1.4 + |5y - 7| = 1.4 + |5(-3) - 7|Replace y with -3. = 1.4 + |-15 - 7| Simplify 5(-3) first. = 1.4 + |-22|Subtract 7 from – 15. = 1.4 + 22|-22| = 22= 23.4Add. EXAMPLE Solve an Absolute Value Equation **2** Solve |x - 18| = 5. Check your solutions. Case 1 a = bCase 2 a = -bor x - 18 = 5x - 18 = -5x - 18 + 18 = -5 + 18x - 18 + 18 = 5 + 18x = 13x = 23|x - 18| = 5|x - 18| = 5CHECK $|23 - 18| \stackrel{?}{=} 5$ $|13 - 18| \stackrel{?}{=} 5$ $|5| \stackrel{?}{=} 5$ $|-5| \stackrel{?}{=} 5$ $5 = 5 \checkmark$ $5 = 5 \checkmark$ The solutions are 23 and 13. Thus, the solution set is {13, 23}. On the number line, we can see that each answer is 5 units away from 18. 5 units 5 units 15 16 17 18 14 19 20 21 22 23 EXAMPLE No Solution **3** Solve |5x - 6| + 9 = 0. |5x - 6| + 9 = 0 Original equation |5x - 6| = -9 Subtract 9 from each side. This sentence is *never* true. So the solution set is \emptyset .

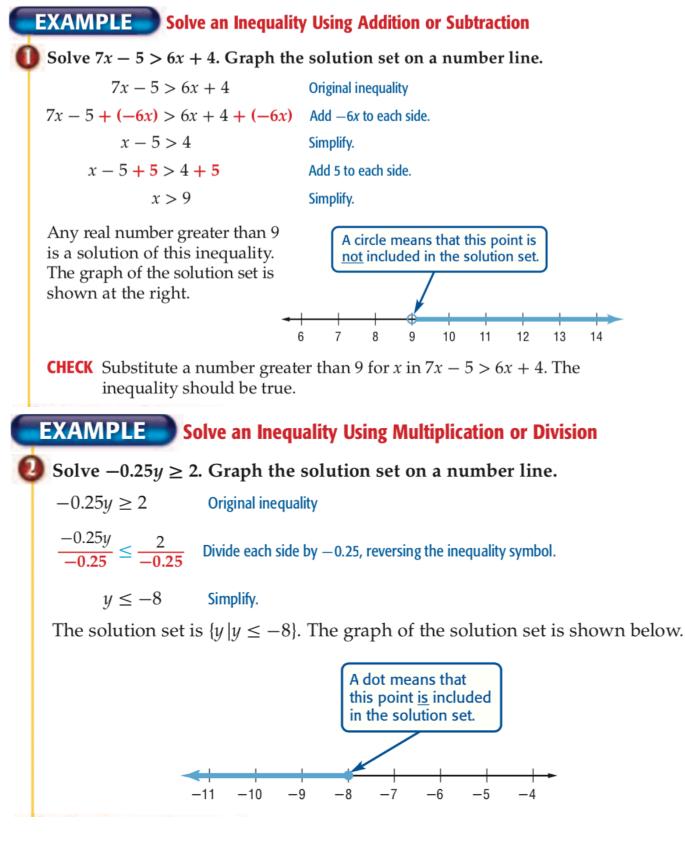
EXAMPLE One Solution Solve |x + 6| = 3x - 2. Check your solutions. Case 1 a = bCase 2 a = -bor x + 6 = -(3x - 2)x + 6 = 3x - 26 = 2x - 2x + 6 = -3x + 28 = 2x4x + 6 = 24 = x4x = -4x = -1There appear to be two solutions, 4 and -1. **CHECK** Substitute each value in the original equation. |x + 6| = 3x - 2|x+6| = 3x - 2 $|4+6| \stackrel{?}{=} 3(4) - 2$ $|-1+6| \stackrel{?}{=} 3(-1) - 2$ $|10| \stackrel{?}{=} 12 - 2$ $|5| \stackrel{?}{=} -3 - 2$ 5 = 5 10 = 10 V Since $5 \neq -5$, the only solution is 4. Thus, the solution set is {4}.

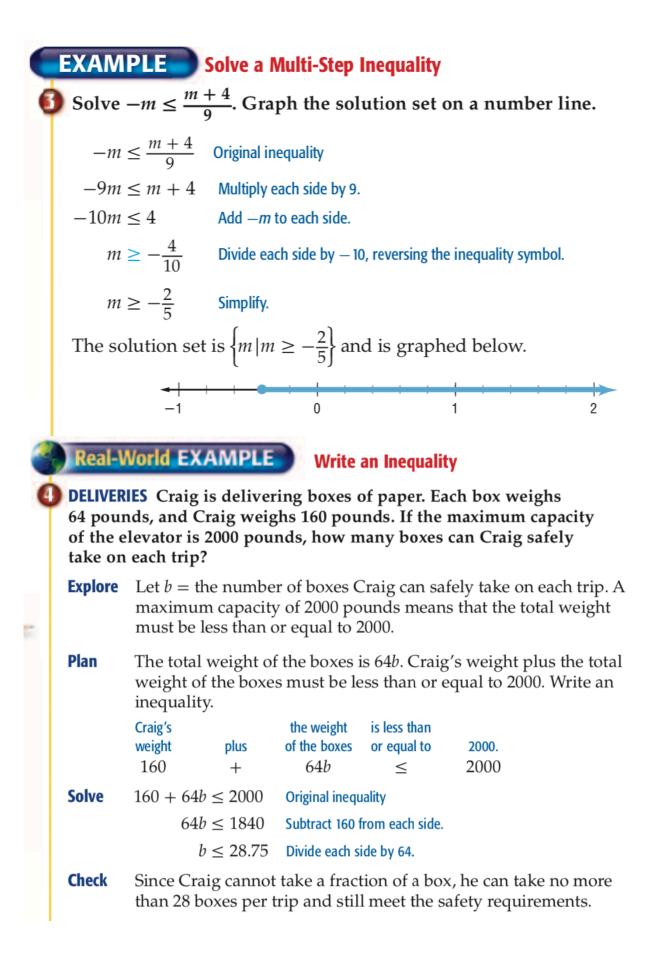
Evaluate each expression if x = -5, y = 3, and z = -2.5.1. |2x|2. |-3y|3. |2x + y|4. |y + 5z|5. -|x + z|6. 8 - |5y - 3|7. 2|x| - 4|2 + y|8. |x + y| - 6|z|

Solve each equation. Check your solutions.

9. |d + 1| = 712. |t + 9| - 8 = 515. 2|y + 4| = 1418. |2c + 3| - 15 = 021. 2|2d - 7| + 1 = 3524. |4y - 5| + 4 = 7y + 8

SOLVING INEQUALITIES





Solve each inequality. Then graph the solution set on a number line.

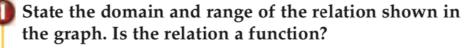
1. $2z + 5 \le 7$ 4. -3x > 66. -33 > 5g + 77. $-3(y - 2) \ge -9$ 9. $5(b - 3) \le b - 7$ 10. 3(2x - 5) < 5(x - 4)12. $2(d + 4) - 5 \ge 5(d + 3)$ 13. 8 - 3t < 4(3 - t)14. $-y < \frac{y + 5}{2}$ 15. $\frac{a + 8}{4} \le \frac{7 + a}{3}$ 16. $-y < \frac{y + 5}{2}$ 18. 6s - (4s + 7) > 5 - s

Define a variable and write an inequality for each problem. Then solve.

- **19**. The product of 7 and a number is greater than 42.
- **20**. The difference of twice a number and 3 is at most 11.
- **21**. The product of -10 and a number is greater than or equal to 20.
- 22. Thirty increased by a number is less than twice the number plus three.

FUNCTIONS AND RELATIONS

EXAMPLE Domain and Range



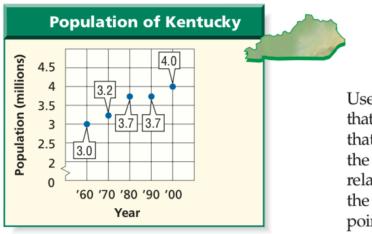
The relation is $\{(-4, 3), (-1, -2), (0, -4), (2, 3), (3, -3)\}$. The domain is $\{-4, -1, 0, 2, 3\}$. The range is $\{-4, -3, -2, 3\}$.

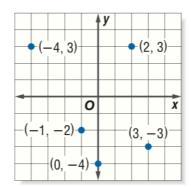
Each member of the domain is paired with exactly one member of the range, so this relation is a function.



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GEOGRAPHY The table shows the population of the state of Kentucky over the last several decades. Graph this information and determine whether it represents a function. Is the relation *discrete* or *continuous*?





Population (millions)	
3.0	
3.2	
3.7	
3.7	
4.0	

Source: U.S. Census Bureau

Use the vertical line test. Notice that no vertical line can be drawn that contains more than one of the data points. Therefore, this relation is a function. Because the graph consists of distinct points, the relation is discrete.

EXAMPLE Graph a Relation

Graph each equation and find the domain and range. Then determine whether the equation is a function and state whether it is *discrete* or *continuous*.

a. y = 2x + 1

Make a table of values to find ordered pairs that satisfy the equation. Choose values for *x* and find the corresponding values for *y*. Then graph the ordered pairs.

Since *x* can be any real number, there is an infinite number of ordered pairs

that can be graphed. All of them lie on the line shown. Notice that every real number is the *x*-coordinate of some point on the line. Also, every real number is the *y*-coordinate of some point on the line. So the domain and range are both all real numbers, and the relation is continuous.

This graph passes the vertical line test. For each *x*-value, there is exactly one *y*-value, so the equation y = 2x + 1 represents a function.

b. $x = y^2 - 2$

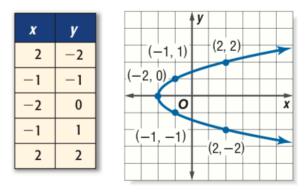
Make a table. In this case, it is easier to choose *y* values and then find the corresponding values for *x*. Then sketch the graph, connecting the points with a smooth curve.

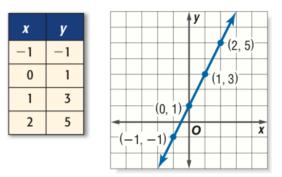
Every real number is the *y*-coordinate of some point on the graph, so the range is all real numbers. But, only

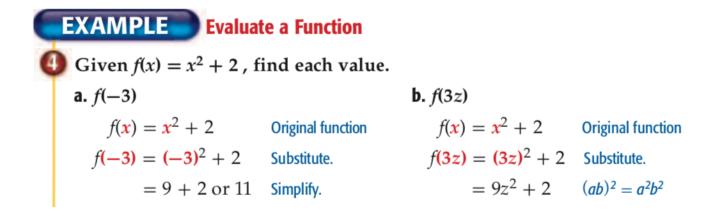
real numbers greater than or equal to -2 are

x-coordinates of points on the graph. So the domain is $\{x | x \ge -2\}$. The relation is continuous.

You can see from the table and the vertical line test that there are two y values for each x value except x = -2. Therefore, the equation $x = y^2 - 2$ does not represent a function.

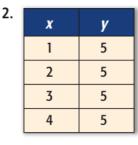


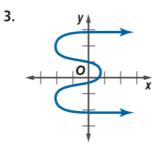




State the domain and range of each relation. Then determine whether each relation is a function. Write *yes* or *no*.

1.	Year	Population
	1970	11,605
	1980	13,468
	1990	15,630
	2000	18,140





Graph each relation or equation and find the domain and range. Then determine whether the relation or equation is a function and state whether *discrete* or *continuous*.

4 . {(1, 2), (2, 3), (3, 4),	(4,5)} 5. {(0,3)	3), (0, 2), (0, 1), (0, 0)}	
7. $y = 2x - 1$	8 . <i>y</i> = 2	$2x^2$	
Find each value if <i>f</i> (<i>x</i>)	= x + 7 and $g(x)$	$x)=(x+1)^2.$	
10. <i>f</i> (2)	11 . <i>f</i> (-4)	12. $f(a + 2)$	13 . g(4)
14 . <i>g</i> (-2)	15 . <i>f</i> (0.5)	16. $g(b-1)$	17 . g(3c)

LINEAR EQUATIONS

EXAMPLE Identify Linear Functions

State whether each function is a linear function. Explain.

- **a.** f(x) = 10 5x This is a linear function because it can be written as f(x) = -5x + 10. m = -5, b = 10
- **b.** $g(x) = x^4 5$ This is not a linear function because *x* has an exponent other than 1.
- **c.** h(x, y) = 2xy This is not a linear function because the two variables are multiplied together.

Real-World EXAMPLE Evaluate a Linear Function

WATER PRESSURE The linear function P(d) = 62.5d + 2117 can be used to find the pressure (lb/ft²) *d* feet below the surface of the water.

a. Find the pressure at a depth of 350 feet.

P(d) = 62.5d + 2117	Original function
P(350) = 62.5(350) + 2117	Substitute.
= 23,992	Simplify.

The pressure at a depth of 350 feet is about $24,000 \text{ lb/ft}^2$.

b. The term 2117 in the function represents the atmospheric pressure at the surface of the water. How many times as great is the pressure at a depth of 350 feet as the pressure at the surface?

Divide the pressure 350 feet down by the pressure at the surface.

 $\frac{23,992}{2117} \approx 11.33$ Use a calculator.

The pressure at that depth is more than 11 times that at the surface.

EXAMPLE Standard Form

Write each equation in standard form. Identify A, B, and C.

a.
$$y = -2x + 3$$

 $y = -2x + 3$ Original equation
 $2x + y = 3$ Add 2x to each side.
So, $A = 2$, $B = 1$, and $C = 3$.
b. $-\frac{3}{5}x = 3y - 2$
 $-\frac{3}{5}x = 3y - 2$ Original equation
 $-\frac{3}{5}x - 3y = -2$ Subtract 3y from each side.
 $3x + 15y = 10$ Multiply each side by -5 so that the coefficients are integers and $A \ge 0$.
So, $A = 3$, $B = 15$, and $C = 10$.

EXAMPLE Use Intercepts to Graph a Line

Find the *x*-intercept and the *y*-intercept of the graph of 3x - 4y + 12 = 0. Then graph the equation.

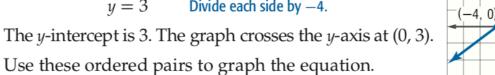
The *x*-intercept is the value of *x* when y = 0.

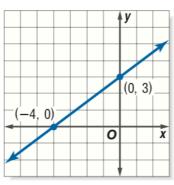
3x - 4y + 12 = 0 Original equation 3x - 4(0) + 12 = 0 Substitute 0 for *y*. 3x = -12 Subtract 12 from each side. x = -4 Divide each side by 3.

The *x*-intercept is -4. The graph crosses the *x*-axis at (-4, 0).

Likewise, the *y*-intercept is the value of *y* when x = 0.

3x - 4y + 12 = 0 Original equation 3(0) - 4y + 12 = 0 Substitute 0 for x. -4y = -12 Subtract 12 from each side. y = 3 Divide each side by -4.





State whether each equation or function is linear. Write *yes* or *no*. If no, explain your reasoning.

1. $\frac{x}{2} - y = 7$ **2.** $\sqrt{x} = y + 5$ **3.** $g(x) = \frac{2}{x - 3}$ **4.** f(x) = 7

Write each equation in standard form. Identify A, B, and C.

5. x + 7 = y8. $y = \frac{2}{3}x + 8$ 9. -0.4x = 1010. 0.75y = -6

Find the *x*-intercept and the *y*-intercept of the graph of each equation. Then graph the equation.

11.
$$2x + y = 6$$

 14. $x = 3y$

 15. $\frac{3}{4}y - x = 1$

 16. $y = -3$

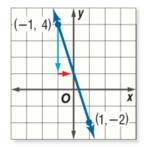
SLOPE

EXAMPLE Find Slope and Use Slope to Graph

Find the slope of the line that passes through (-1, 4) and (1, -2). Then graph the line.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
 Slope formula
= $\frac{-2 - 4}{1 - (-1)}$ $(x_1, y_1) = (-1, 4), (x_2, y_2) = (1, -2)$
= $\frac{-6}{2}$ or -3 The slope is -3 .

Graph the two ordered pairs and draw the line. Use the slope to check your graph by selecting any point on the line. Then go down 3 units and right 1 unit or go up 3 units and left 1 unit. This point should also be on the line.



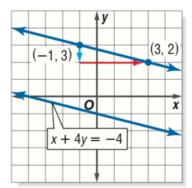
EXAMPLE Parallel Lines

Graph the line through (-1, 3) that is parallel to the line with equation x + 4y = -4.

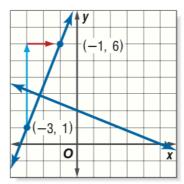
The *x*-intercept is -4, and the *y*-intercept is -1. Use the intercepts to graph x + 4y = -4.

The line falls 1 unit for every 4 units it moves to the right, so the slope is $-\frac{1}{4}$.

Now use the slope and the point at (-1, 3) to graph the line parallel to the graph of x + 4y = -4.



EXAMPLE Perpendicular Lines



Graph the line through (-3, 1) that is perpendicular to the line with equation 2x + 5y = 10.

The *x*-intercept is 5, and the *y*-intercept is 2. Use the intercepts to graph 2x + 5y = 10.

The line falls 2 units for every 5 units it moves to

the right, so the slope is $-\frac{2}{5}$. The slope of the perpendicular line is the opposite reciprocal of $-\frac{2}{5}$, or $\frac{5}{2}$.

Start at (-3, 1) and go up 5 units and right 2 units. Use this point and (-3, 1) to graph the line.

Find the slope of the line that passes through each pair of points.

1. (0, 3), (5, 0)**2.** (2, 3), (5, 7)**3.** (2, 8), (2, -8)

Graph the line passing through the given point with the given slope.

7. (0, 3); 1 **8.** (2, 3); 0 **9.** (-1, 1); $-\frac{1}{3}$

Graph the line that satisfies each set of conditions.

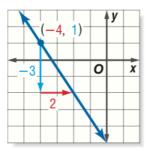
- **10**. passes through (0, 1), parallel to a line with a slope of -2
- **11**. passes through (4, -5), perpendicular to the graph of -2x + 5y = 1

WRITING LINEAR EQUATIONS

EXAMPLE Write an Equation Given Slope and a Point

Write an equation in slope-intercept form for the line that has a slope of $-\frac{3}{2}$ and passes through (-4, 1).

y = mx + b $1 = -\frac{3}{2}(-4) + b$ 1 = 6 + b -5 = bSlope-intercept form $(x, y) = (-4, 1), m = -\frac{3}{2}$ Simplify.



The equation in slope-intercept form is $y = -\frac{3}{2}x - 5$.

STANDARDIZED TEST EXAMPLE Write an Equation Given Two Points

What is an equation of the line through (-1, 4) and (-4, 5)?

A $y = -\frac{1}{3}x + \frac{11}{3}$ **B** $y = \frac{1}{3}x + \frac{13}{3}$ **C** $y = -\frac{1}{3}x + \frac{13}{3}$ **D** y = -3x + 1

Read the Test Item

You are given the coordinates of two points on the line.

Solve the Test Item

First, find the slope of the line.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
 Slope formula
= $\frac{5 - 4}{-4 - (-1)}$ $(x_{\nu} y_1) = (-1, 4),$
 $(x_{2\nu} y_2) = (-4, 5)$
= $\frac{1}{-3}$ or $-\frac{1}{3}$ Simplify.

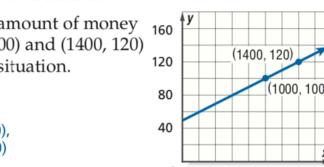
Then write an equation.

$$y - y_1 = m(x - x_1)$$
Point-slope form
$$y - 4 = -\frac{1}{3} [x - (-1)]$$

$$m = -\frac{1}{3}; \text{ use either point for } (x_1, y_1).$$

$$y = -\frac{1}{3}x + \frac{11}{3}$$
The answer is A.

Real-World EXAMPLE

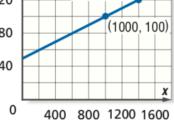


SALES As a salesperson, Eric Fu is paid a daily salary plus commission. When his sales are \$1000, he makes \$100. When his sales are \$1400, he makes \$120.

a. Write a linear equation to model this situation.

Let *x* be his sales and let *y* be the amount of money he makes. Use the points (1000, 100) and (1400, 120) to make a graph to represent the situation.

 $m = \frac{y_2 - y_1}{x_2 - x_1}$ Slope formula $=\frac{120-100}{1400-1000} \quad \begin{array}{l} (x_1, y_1) = (1000, 100), \\ (x_2, y_2) = (1400, 120) \end{array}$ = 0.05Simplify.



Now use the slope and either of the given points with the point-slope form to write the equation.

 $y - y_1 = m(x - x_1)$ Point-slope form y - 100 = 0.05(x - 1000) $m = 0.05, (x_1, y_1) = (1000, 100)$ y - 100 = 0.05x - 50Distributive Property y = 0.05x + 50 Add 100 to each side.

The slope-intercept form of the equation is y = 0.05x + 50.

b. What are Mr. Fu's daily salary and commission rate?

The *y*-intercept of the line is 50. The *y*-intercept represents the money Eric would make if he had no sales. In other words, \$50 is his daily salary. The slope of the line is 0.05. Since the slope is the coefficient of x, which is his sales, he makes 5% commission.

c. How much would Mr. Fu make in a day if his sales were \$2000?

Find the value of *y* when x = 2000.

y = 0.05x + 50Use the equation you found in part **a**.

= 0.05(2000) + 50 Replace x with 2000.

= 100 + 50 or 150Simplify.

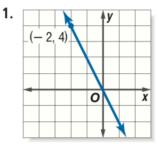
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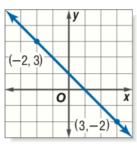
Mr. Fu would make \$150 if his sales were \$2000.

EXAMPLE Write an Equation of a Perpendicular Line

Write an equation for the line that passes through (-4, 3) and is perpendicular to the line whose equation is y = -4x - 1. The slope of the given line is -4. Since the slopes of perpendicular lines are opposite reciprocals, the slope of the perpendicular line is $\frac{1}{4}$. Use the point-slope form and the ordered pair (-4, 3). $y - y_1 = m(x - x_1)$ Point-slope form $y - 3 = \frac{1}{4}[x - (-4)]$ $(x_1, y_1) = (-4, 3), m = \frac{1}{4}$ $y - 3 = \frac{1}{4}x + 1$ Distributive Property $y = \frac{1}{4}x + 4$ Add 3 to each side.

Write an equation in slope-intercept form for each graph.





2.

Write an equation in slope-intercept form for the line that satisfies each set of conditions.

3. slope -1, passes through (7, 2)

4. slope $\frac{3}{4}$, passes through the origin

0

x

- **5**. passes through (1, -3) and (-1, 2)
- **6**. *x*-intercept -5, *y*-intercept 2
- 7. passes through (1, 1), parallel to the graph of 2x + 3y = 5
- **8**. passes through (0, 0), perpendicular to the graph of 2y + 3x = 4

SOLVING SYSTEMS OF EQUATIONS

EXAMPLE Solve the System of Equations by Completing a Table

Solve the system of equations by completing a table.

$$-2x + 2y = 4$$
$$-4x + y = -1$$

Write each equation in slope-intercept form.

$$-2x + 2y = 4 \quad \rightarrow \quad y = x + 2$$

$$-4x + y = -1 \rightarrow y = 4x - 1$$

Use a table to find the solution that satisfies both equations.

x	$y_1 = x + 2$	<i>y</i> ₁	$y_2 = 4x - 1$	<i>y</i> ₂	(x, y_1)	(x, y_2)
-1	$y_1 = (-1) + 2$	1	$y_2 = 4(-1) - 1$	-5	(-1, 1)	(-1, -5)
0	$y_1 = 0 + 2$	2	$y_2 = 4(0) - 1$	-1	(0, 2)	(0, -1)
1	$y_1 = (1) + 2$	3	$y_2 = 4(1) - 1$	3	(1, 3)	(1, 3)

The solution of the system is (1, 3).

The solution of the system of equations is the ordered pair that satisfies both equations.

EXAMPLE Solve by Graphing

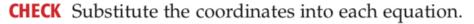
Solve the system of equations by graphing. 2x + y = 5

x - y = 1

Write each equation in slope-intercept form.

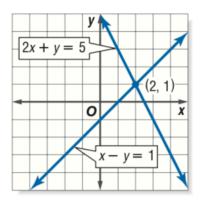
$$2x + y = 5 \quad \rightarrow \quad y = -2x + 5$$
$$x - y = 1 \quad \rightarrow \quad y = x - 1$$

The graphs appear to intersect at (2, 1).



2x + y = 5	x - y = 1	Original equations
2 (2) + 1 ² = 5	2 − 1 [?] = 1	Replace <i>x</i> with 2 and <i>y</i> with 1.
5 = 5 v	1 = 1 🖌	Simplify.

The solution of the system is (2, 1).



EXAMPLE Intersecting Lines

Graph the system of equations and describe it as consistent and independent, consistent and dependent, or inconsistent.

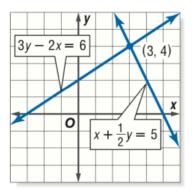
$$x + \frac{1}{2}y = 5$$
$$3y - 2x = 6$$

Write each equation in slope-intercept form.

$$x + \frac{1}{2}y = 5 \quad \rightarrow \quad y = -2x + 10$$

$$3y - 2x = 6 \quad \rightarrow \quad y = \frac{2}{3}x + 2$$

The graphs intersect at (3, 4). Since there is one solution, this system is *consistent and independent*.



EXAMPLE Same Line

Graph the system of equations and describe it as *consistent* and *independent*, *consistent* and *dependent*, or *inconsistent*.

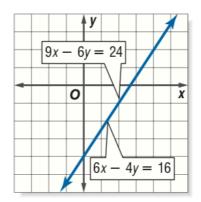
$$9x - 6y = 24$$
$$6x - 4y = 16$$

Write each equation in slope-intercept form.

$$9x - 6y = 24 \quad \rightarrow \quad y = \frac{3}{2}x - 4$$
$$6x - 4y = 16 \quad \rightarrow \quad y = \frac{3}{2}x - 4$$

Since the equations are equivalent, their graphs are the same line. Any ordered pair representing a point on that line will satisfy both equations.

So, there are infinitely many solutions to this system. It is *consistent and dependent*.



EXAMPLE Parallel Lines

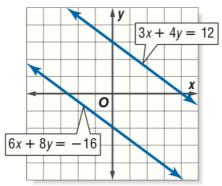
Graph the system of equations and describe it as consistent and independent, consistent and dependent, or inconsistent.

$$3x + 4y = 12$$

$$6x + 8y = -16$$

$$3x + 4y = 12 \quad \rightarrow \quad y = -\frac{3}{4}x + 3$$

$$6x + 8y = -16 \quad \rightarrow \quad y = -\frac{3}{4}x - 2$$



The lines do not intersect. Their graphs are parallel lines. So, there are no solutions that satisfy both equations. This system is *inconsistent*.

EXAMPLE Solve by Using Substitution

Use substitution to solve the system of equations.

$$x + 2y = 8$$
$$\frac{1}{2}x - y = 18$$

1

1

Solve the first equation for *x* in terms of *y*.

x + 2y = 8 First equation x = 8 - 2y Subtract 2y from each side.

Substitute 8 - 2y for x in the second equation and solve for y.

 $\frac{1}{2}x - y = 18$ Second equation $\frac{1}{2}(8 - 2y) - y = 18$ Substitute 8 - 2y for x. 4 - y - y = 18 Distributive Property -2y = 14 Subtract 4 from each side. y = -7 Divide each side by -2. Now, substitute the value for *y* in either original equation and solve for *x*.

x + 2y = 8 First equation

x + 2(-7) = 8 Replace *y* with -7.

x - 14 = 8 Simplify.

x = 22

The solution of the system is (22, -7).

STANDARDIZED TEST EXAMPLE Solve by Substitution

Matthew stopped for gasoline twice on a long car trip. The price of gasoline at the first station where he stopped was \$2.56 per gallon. At the second station, the price was \$2.65 per gallon. Matthew bought a total of 36.1 gallons of gasoline and spent \$94.00. How many gallons of gasoline did Matthew buy at the first gas station?
A 17.6 B 18.5 C 19.2 D 20.1

Read the Item

You are asked to find the number of gallons of gasoline that Matthew bought at the first gas station.

Solve the Item

Step 1 Define variables and write the system of equations. Let *x* represent the number of gallons bought at the first station and *y* represent the number of gallons bought at the second station.

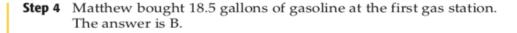
x + y = 36.1 The total number of gallons was 36.1. 2.56x + 2.65y = 94 The total price was \$94.

Step 2 Solve one of the equations for one of the variables in terms of the other. Since the coefficient of *y* is 1 and you are asked to find the value of *x*, it makes sense to solve the first equation for *y* in terms of *x*.

x + y = 36.1 First equation y = 36.1 - x Subtract x from each side.

Step 3 Substitute 36.1 - x for *y* in the second equation.

2.56x + 2.65y = 94	Second equation
2.56x + 2.65(36.1 - x) = 94	Substitute 36.1 — x for y .
2.56x + 95.665 - 2.65x = 94	Distributive Property
-0.09x = -1.665	Simplify.
x = 18.5	Divide each side by -0.09.



EXAMPLE Solve by Using Elimination

Use the elimination method to solve the system of equations.

4a + 2b = 152a + 2b = 7

-

In each equation, the coefficient of *b* is 2. If one equation is subtracted from the other, the variable *b* will be eliminated.

4a + 2b = 15 (-) 2a + 2b = 7 2a = 8Subtract the equations. a = 4Divide each side by 2.

Now find *b* by substituting 4 for *a* in either original equation.

2a + 2b = 7 Second equation 2(4) + 2b = 7 Replace *a* with 4. 8 + 2b = 7 Multiply. 2b = -1 Subtract 8 from each side. $b = -\frac{1}{2}$ Divide each side by 2. The solution is $\left(4, -\frac{1}{2}\right)$.

EXAMPLE Multiply, Then Use Elimination

Use the elimination method to solve the system of equations.

3x - 7y = -145x + 2y = 45

-

Multiply the first equation by 2 and the second equation by 7. Then add the equations to eliminate the *y* variable.

3x - 7y = -14 5x + 2y = 45 (+) 35x + 14y = 315 41x = 287 x = 7 (+) 35x + 14y = 315 41x = 287 x = 7 (+) 35x + 14y = 315 41x = 287 x = 7 (+) 35x + 14y = 315 x = 7 (+) 35x + 14y = 315 x = 7 (+) 35x + 14y = 315 x = 7 (+) 35x + 14y = 315 x = 7 (+) 35x + 14y = 315 x = 7 (+) 35x + 14y = 315 (+) 35x + 14y = 315

Replace *x* with 7 and solve for *y*.

3x - 7y = -14 First equation

 $3(7) - 7y = -14 \quad \text{Replace } x \text{ with 7.}$ $21 - 7y = -14 \quad \text{Multiply.}$ $-7y = -35 \quad \text{Subtract 21 from each side.}$ $y = 5 \quad \text{Divide each side by } -7.$

The solution is (7, 5).

EXAMPLE Inconsistent System

Use the elimination method to solve the system of equations.

8x + 2y = 17 -4x - y = 9Use multiplication to eliminate *x*. 8x + 2y = 17 -4x - y = 9Multiply by 2. 8x + 2y = 17 -8x - 2y = 18 0 = 35Add the equations.

Since there are no values of *x* and *y* that will make the equation 0 = 35 true, there are no solutions for this system of equations.

Solve each system of equations by graphing or by completing a table.

3. 2x + 6y = 6 $\frac{1}{3}x + y = 1$

Solve each system of equations by using substitution.

1. $2x + 3y = 10$	2. $x = 4y - 10$	3. $3x - 4y = -27$
x + 6y = 32	5x + 3y = -4	2x + y = -7

Solve each system of equations by using elimination.

4. $7x + y = 9$	5. $r + 5s = -17$	6. $6p + 8q = 20$
5x - y = 15	2r - 6s = -2	5p - 4q = -26